

# Universal hardness and elastic recovery in Vickers nanoindentation of copper phosphate and silicate glasses

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## Abstract

Load/unload displacement (penetration) curves for  $y\text{CuO}_x \cdot (100-y)\text{P}_2\text{O}_5$  glasses ( $y=45, 50$ ) with different copper valence states, silica and soda-lime silicate glasses at room temperature (humidity  $\sim 64\%$ ) have been measured using a Vickers nanoindentation technique, and universal hardness  $H_u$  and elastic recovery  $E_R$  have been estimated in the load range of 0.1–1 N. Copper phosphate glasses have the values of  $H_u=1.7\text{--}2.5$  GPa and  $E_R=0.55\text{--}0.65$ , depending on the  $\text{Cu}^+/\text{Cu}^{2+}$  ratio. The glasses with high  $\text{Cu}^+$  contents show large densifications (plastic deformation) during loading and small elastic recoveries during unloading compared with the glasses with no  $\text{Cu}^+$  ions. These deformation behaviors are well explained qualitatively by considering lower coordination number and more covalent bonding of  $\text{Cu}^+$  compared with  $\text{Cu}^{2+}$ , which have been confirmed from X-ray photoelectron spectra. Silica glass has  $E_R=0.77$ , which is large compared with  $E_R=0.63$  in a soda-lime silicate glass. This large difference leads to the smaller value in  $H_u$  of silica glass than that of a soda-lime silica glass. It is confirmed that load displacement curves in nanoindentation tests are well fitted with quadratic equations. © 2002 Elsevier Science Ltd. All rights reserved.

**Keywords:** Copper phosphate; Glass; Hardness; Nanoindentation; Silicate

## 1. Introduction

When a sharp indenter such as Vickers indenter is loaded onto a glass, a residual surface impression is observed after unloading, and the material hardness is conveniently estimated from the projected area of the impression. It is known that some extent of deformation during loading is recovered during unloading, i.e., elastic recovery.<sup>1,2</sup> Since it is expected that the degree of elastic recovery depends on glass systems and glass compositions, the hardness evaluated from a residual surface impression after unloading is insufficient for an in-depth understanding of deformation behaviors in glass. In this point of view, it is also important to evaluate the hardness during loading, i.e., the so-called “universal hardness”. So far, numerous studies of mechanical and elastic properties of glasses such as Vickers hardness and Young’s modulus have been carried out, but reports on the elastic recovery of glasses

and universal hardness are small.<sup>1–7</sup> On the other hand, irreversible (non-recoverable) deformation in indentation tests has been regarded as plastic (shear) deformation, which is divided into two deformation components: densification and plastic flow.<sup>8–10</sup> Therefore, in order to understand the deformation mechanism in glass, it is necessary to clarify contributions of densification and plastic flow to plastic deformation.

Glasses containing copper have various attractive points such as high- $T_c$  superconducting precursors, semiconducting, superionic conducting, very low thermal expansion, laser and optical nonlinear glasses. Copper can exist in glasses as cuprous  $\text{Cu}^+$  or cupric  $\text{Cu}^{2+}$  ions, and it is known that the valence state in copper affects not only chemical/physical properties but also the glass-forming ability.<sup>11,12</sup> Very recently, the present authors’ group found that  $\text{CuO-P}_2\text{O}_5$  glasses show extremely unusual elastic and mechanical properties depending on the  $\text{Cu}^+/\text{Cu}^{2+}$  ratio.<sup>13</sup> Particularly, some glasses with high  $\text{Cu}^+/\text{Cu}^{2+}$  ratios have a large fracture toughness of  $K_c=1.1$  MPam<sup>1/2</sup>, indicating a high resistance against crack formation in Vickers indentation tests. They proposed that the unusual elastic and mechanical properties

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of copper phosphate glasses are explained qualitatively by considering unique oxygen coordination and bonding states of  $\text{Cu}^+$  ions, i.e., lower coordination number and more covalent bonding compared with  $\text{Cu}^{2+}$  ions. It is of particular interest to examine universal hardness, elastic recovery and plastic deformation and to clarify the deformation mechanism in copper phosphate glasses more in detail. Furthermore, it is desired to clarify the bonding state of  $\text{Cu}^+$  ions in copper phosphate glasses and to demonstrate the structure and bonding role of  $\text{Cu}^+$  ions proposed in the previous papers.<sup>12,13</sup>

In the present study, firstly the chemical bonding state of  $\text{Cu}^+$  ions in  $y\text{CuO}_x \cdot (100-y)\text{P}_2\text{O}_5$  glasses ( $y=45, 50$ ) with different copper valence states, i.e.,  $R(\text{Cu}^+) = \text{Cu}^+ / (\text{Cu}^+ + \text{Cu}^{2+})$ , was clarified from X-ray photoelectron spectroscopy (XPS), and then universal hardness, elastic recovery and plastic deformation were examined by a Vickers nanoindentation technique. To the best of our knowledge, the data on universal hardness and elastic recovery of silica and soda-lime silicate glasses which are most important and standard glasses are also insufficient, and therefore nanoindentation experiments were carried out for those glasses in this study. The deformation mechanism in copper phosphate glasses was compared with those of silica and soda-lime silicate glasses. Such information will lead to designs of less-brittle glasses.

## 2. Experimental procedure

The nominal compositions examined in the present study are  $y\text{CuO}_x \cdot (100-y)\text{P}_2\text{O}_5$  ( $y=45, 50$ ). A mixture of reagent grades of  $\text{CuO}$  and  $\text{H}_3\text{PO}_4$  was reacted and dried at 200 °C for 2 h and melted in an alumina crucible at 1200 °C for 30 min in an electric furnace. The batch weight was 20 g. The melts were poured onto an iron plate and pressed quickly to a thickness of 1–2 mm. The glasses were ground, and glucose (1–4 wt.%) was added to control the copper valence state. The mixture was remelted in a covered alumina crucible at 1200 °C for 10 min in an electric furnace. The melts were cast on an iron plate heated to 150 °C. The bulk glasses were annealed at temperatures of  $T_g + 10$  K for 15 min to release internal stress. Glass transition temperatures,  $T_g$ , were determined by using differential thermal analysis (DTA) at a heating rate of 10 K/min.  $\text{Cu}^+$  contents in the glasses, i.e.  $R(\text{Cu}^+) = \text{Cu}^+ / (\text{Cu}^+ + \text{Cu}^{2+})$ , were analyzed by cerate titration within an accuracy of  $\pm 5\%$ .<sup>12</sup> Fused silica glass was obtained from Asahi Glass company, and a soda-lime silicate glass ( $\sim 12.7\text{Na}_2\text{O} \cdot 5.9\text{MgO} \cdot 9.4\text{CaO} \cdot 0.9\text{Al}_2\text{O}_3 \cdot 71.0\text{SiO}_2$  mol%) was obtained from Nippon Sheet Glass company.

XPS measurements were carried out using a SHIMADZU ESCA-3200 electron spectrometer which has Al conical anode for charge control. Non-monochromatic

240 W Mg- $K_\alpha$  X-ray provided the excitation radiation. During experiments the pressure inside the analyzer chamber was  $\sim 10^{-7}$  Pa. XPS spectra of O1s (oxygen) core level of fresh glass surfaces were recorded. Drift of the electron binding energy due to surface charging effect was calibrated by utilizing the C1s (carbon) peak of the contamination of the pumping oil at sample introduction chamber ( $E_B = 284.6$  eV).

Universal hardness during loading and the fraction of elastic recovery after unloading were evaluated from load/unload displacement curves obtained using a nanoindentation apparatus (Akashi, MZT-4). Measurements were carried out at room temperature in air (relative humidity was  $\sim 64\%$ ). Fig. 1 shows a schematic load/unload displacement curve for a nonflat indenter with definitions of load  $P$ , indentation depth  $h$ , the peak indentation load  $P_{\text{max}}$ , the indenter displacement at peak load  $h_t$ , and the final depth of the contact impression after unloading  $h_f$ . In this study, a Vickers indenter was used. The load and unload speed was 49 mN/s and the maximum load was  $\sim 980$  mN. Within this maximum load, any crack is not observed during Vickers indentations.<sup>13</sup> The displacement (penetration depth) during loading gives universal hardness,  $H_u$ , which is expressed by the following equation.

$$H_u = \frac{P_{\text{max}}}{26.43h_t^2} \quad (1)$$

The elastic recovery,  $E_R$ , corresponds to the area ratio in the indentation hysteresis loop, i.e., the ratio of the recovered area ( $h_f - A - h_t$ ) and the total area ( $0 - A - h_t$ ). Since the product of load  $P$  (N) and displacement  $h$  (m) has a dimension of energy (J), the elastic recovery means the fraction of the consumed energy for elastic deformation to the consumed energy for total (elastic + plastic) deformation.

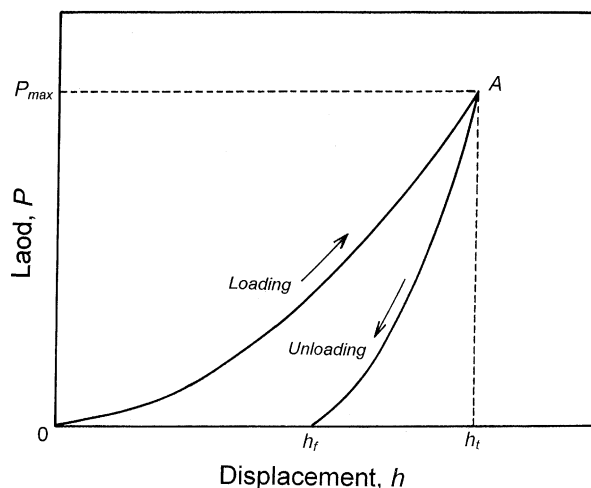


Fig. 1. A schematic load/unload displacement curve in a nonflat indentation experiment for elastoplastic materials.  $P_{\text{max}}$ ,  $h_t$ ,  $h_f$  are the peak indentation load, the indenter displacement at peak load, and the final depth of the contact impression after unloading, respectively.

Table 1

Values of copper valence ratio  $R(\text{Cu}^+) = \text{Cu}^+ / (\text{Cu}^+ + \text{Cu}^{2+})$ , glass transition temperature  $T_g$ , density  $d$ , mean atomic volume  $V_m$ , usual Vickers hardness  $H_v$ , Young's modulus  $E$ , and fracture toughness  $K_c$  for  $y\text{CuO}_x \cdot (100-y)\text{P}_2\text{O}_5$  glasses

Glass	$R(\text{Cu}^+)$ $\pm 0.03$	$T_g$ (°C) $\pm 2$	$d$ (g/cm <sup>3</sup> ) $\pm 0.01$	$V_m$ (cm <sup>3</sup> /g-atom) $\pm 0.02$	$H_v$ (GPa) $\pm 0.1$	$E$ (GPa) $\pm 0.1$	$K_c$ (MPa.m <sup>1/2</sup> )
$y=45$	0.00	431	3.21	7.46	4.3	66.8	$0.92 \pm 0.04$
	0.57	218	3.17	7.63	2.7	50.6	$0.91 \pm 0.06$
$y=50$	0.00	431	3.32	7.41	4.4	72.9	$0.72 \pm 0.04$
	0.43	279	3.28	7.56	3.4	60.4	$1.14 \pm 0.05$

The values of  $H_v$ ,  $E$ , and  $K_c$  are taken from our previous paper.<sup>13</sup>

### 3. Results

The values of  $T_g$  and  $R(\text{Cu}^+) = \text{Cu}^+ / (\text{Cu}^+ + \text{Cu}^{2+})$  for copper phosphate glasses examined in the present study are summarized in Table 1, in which the values of mean atomic volume, Young's modulus  $E$ , Vickers hardness  $H_v$ , and fracture toughness  $K_c$  reported in the previous paper<sup>13</sup> are also given. As reported by Sato et al.,<sup>12</sup> the change in chemical compositions during the melting for glass preparation is very small and the contamination of alumina from the crucible is about 1 mol%, irrespective of the amount of glucose. It was confirmed from infrared (IR) spectroscopy that some

amounts of OH groups are present in all glasses prepared in the present study. Although quantitative analyses have not been conducted, the intensity of the absorption peaks at around 3000 cm<sup>-1</sup> due to OH groups is not so strong.

#### 3.1. Bonding state of $\text{Cu}^+$ in copper phosphate glasses

The XPS spectra near the O1s levels obtained for  $45\text{CuO}_x \cdot 55\text{P}_2\text{O}_5$  glasses are shown in Fig. 2. Similar XPS spectra were obtained for  $50\text{CuO}_x \cdot 50\text{P}_2\text{O}_5$  glasses. It is observed that the O1s spectra have asymmetric peaks. The spectra shown in Fig. 2 were fitted to decompose the asymmetric peaks by a sum of Gaussian curves by means of least square method with a linear background subtraction. As shown in Fig. 2, the oxygen 1s (O1s) signal in the spectra of  $45\text{CuO}_x \cdot 55\text{P}_2\text{O}_5$  glasses can be decomposed into two components denoted in the text as O1s(1) and O1s(2) with a good fitting quality. The maximum peaks are observed at  $\sim 534$  eV for O1s(1) and at  $\sim 532$  eV for O1s(2). The fraction of O1s(1) peak intensity in the O1s spectra is plotted as a function of  $R(\text{Cu}^+)$  in Fig. 3, showing almost a linear correlation between them.

XPS spectra for some alkali phosphate and zinc phosphate glasses have been reported, and it has been well analyzed that the high binding energy peak near 534 eV is related to bridging oxygens that link neighboring phosphorus atoms in  $\text{PO}_4$  tetrahedra and the low binding energy peak near 532 eV corresponds to non-bridging oxygens and oxygens with double bonds, giving a quantitative measure of the ratio of bridging and non-bridging oxygens.<sup>14–16</sup> XPS studies for copper phosphate and sodium copper phosphate glasses have been reported, but the valence state of copper ions in those glasses are unclear.<sup>17,18</sup>

By assuming that  $\text{Cu}^{2+}$  ions in copper phosphate glasses create only non-bridging oxygens and on the other hand  $\text{Cu}^+$  ions create only bridging oxygens, the fraction of bridging oxygens in copper phosphate glasses was calculated as a function of  $R(\text{Cu}^+)$ . The results are shown in Fig. 3. It is seen that the data on the fraction of O1s(1) peak intensity estimated from XPS spectra lie well on the calculated lines (solid lines in Fig. 3).

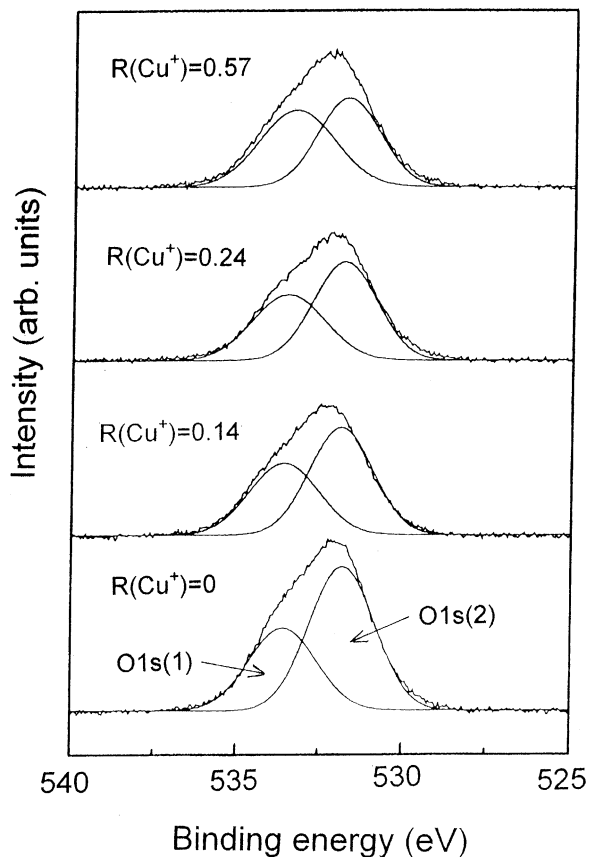


Fig. 2. Oxygen 1s photoelectron spectra at room temperature for  $45\text{CuO}_x \cdot 55\text{P}_2\text{O}_5$  glasses with different copper valence states,  $R(\text{Cu}^+) = \text{Cu}^+ / (\text{Cu}^+ + \text{Cu}^{2+})$ .

The XPS spectra shown in Fig. 2, therefore, support the structure and bonding model for the role of copper ions in copper phosphate glasses proposed in the previous papers.<sup>12,13</sup> That is,  $\text{Cu}^+$  ions in copper phosphate glasses are surrounded by two oxygen atoms through covalent bond and bridge two phosphate chains. The structural and bonding roles of  $\text{Cu}^+$  and  $\text{Cu}^{2+}$  ions in copper phosphate glasses are completely different.

### 3.2. Universal hardness and elastic recovery

The load/unload displacement curves at various maximum loads for  $50\text{CuO}_x \cdot 50\text{P}_2\text{O}_5$  glass with  $R(\text{Cu}^+) = 0.43$  are shown in Fig. 4 as a typical example. Similar load/unload displacement curves were obtained for other copper phosphate, silica and soda-lime silicate glasses. The values of universal hardness  $H_u$  and elastic recovery  $E_R$  estimated from the load/unload displacement curves for copper phosphate, silica, soda-lime silicate glasses are shown in Figs. 5 and 6 as a function of  $P_{\text{max}}$ , respectively. The following features are obtained. In copper phosphate glasses, the  $H_u$  values are 1.7–2.5 GPa and increase slightly with decreasing load.  $50\text{CuO}_x \cdot 50\text{P}_2\text{O}_5$  glasses have higher  $H_u$  values compared with  $45\text{CuO}_x \cdot 55\text{P}_2\text{O}_5$  glasses. The glasses with  $R(\text{Cu}^+) = 0.43$  and  $0.57$  have slightly large  $H_u$  values compared with the glasses with  $R(\text{Cu}^+) = 0$ . The  $E_R$  values are 0.55–0.65 and decrease gradually with decreasing load. The elastic recovery depends strongly on the  $\text{Cu}^+/\text{Cu}^{2+}$  ratio. That is, the  $E_R$  values in the glasses with  $R(\text{Cu}^+) = 0.43$  and  $0.57$  are much smaller

than those in the glasses with  $R(\text{Cu}^+) = 0$ . In silica and soda-lime silicate glasses, the  $H_u$  values depend strongly on the load, and silica glass has smaller  $H_u$  values compared with a soda-lime silicate glass. Silica glass has the  $E_R$  values of  $\sim 0.77$ , which are larger than the  $E_R$  values of  $\sim 0.63$  in a soda-lime silicate glass. These results demonstrate that the universal hardness and elastic recovery are very sensitive to glass systems and compositions.

As shown in Fig. 5, the universal hardness increases with decreasing load. This phenomenon is known as

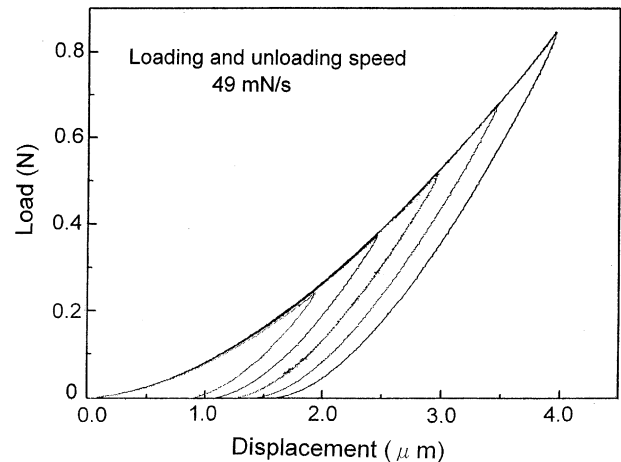


Fig. 4. Load/unload displacement curves at room temperature in air for  $50\text{CuO}_x \cdot 50\text{P}_2\text{O}_5$  glass with  $R(\text{Cu}^+) = 0.43$ . The load and unload speed was 49 mN/s.

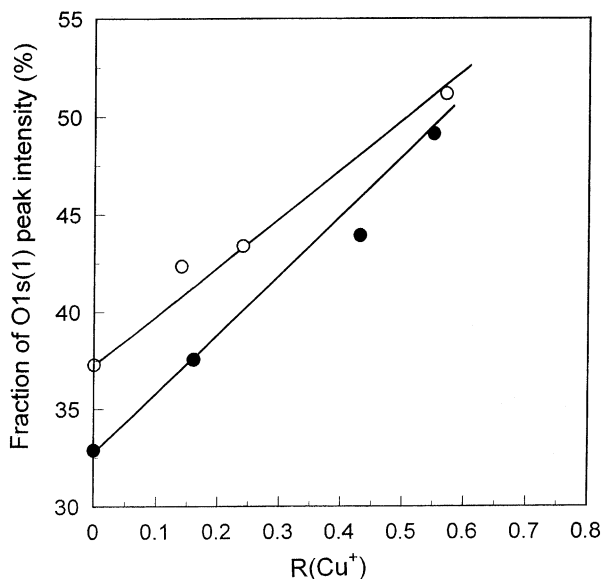


Fig. 3. Fractions of O1s(1) component in oxygen 1s photoelectron spectra for  $y\text{CuO}_x \cdot (100-y)\text{P}_2\text{O}_5$  glasses with  $y = 45$  and  $50$  as a function of copper valence states,  $R(\text{Cu}^+) = \text{Cu}^+ / (\text{Cu}^+ + \text{Cu}^{2+})$ . The solid lines represent the fraction of bridging oxygens calculated by assuming that  $\text{Cu}^{2+}$  ions create only non-bridging oxygens and  $\text{Cu}^+$  ions create only bridging oxygens.  $\circ$ :  $y = 45$ ,  $\bullet$ :  $y = 50$ .

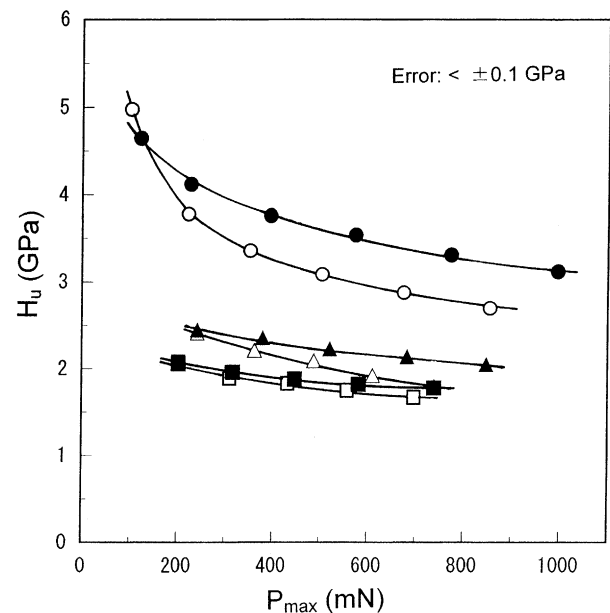


Fig. 5. Correlation between the maximum load  $P_{\text{max}}$  and universal hardness  $H_u$  for copper phosphate, silica and soda-lime silicate glasses.  $\circ$ : silica,  $\bullet$ : soda-lime silicate,  $\square$ :  $45\text{CuO}_x \cdot 55\text{P}_2\text{O}_5$  with  $R(\text{Cu}^+) = 0$ ,  $\blacksquare$ :  $45\text{CuO}_x \cdot 55\text{P}_2\text{O}_5$  with  $R(\text{Cu}^+) = 0.57$ ,  $\triangle$ :  $50\text{CuO}_x \cdot 50\text{P}_2\text{O}_5$  with  $R(\text{Cu}^+) = 0$ ,  $\blacktriangle$ :  $50\text{CuO}_x \cdot 50\text{P}_2\text{O}_5$  with  $R(\text{Cu}^+) = 0.43$ .

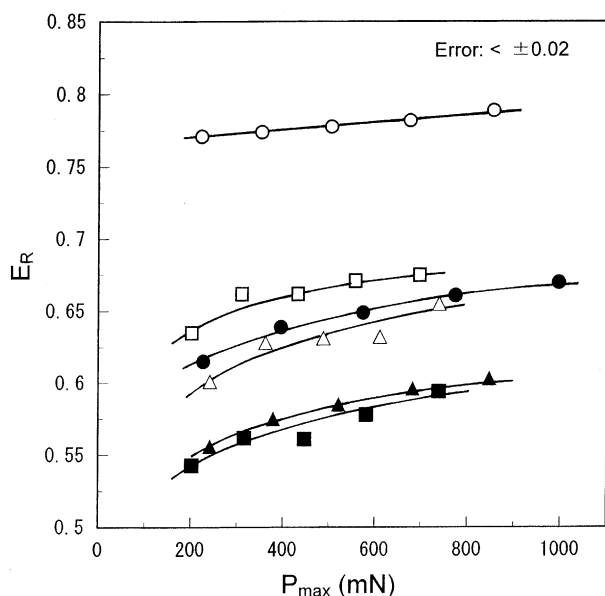


Fig. 6. Correlation between the maximum load  $P_{\max}$  and elastic recovery  $E_R$  for copper phosphate, silica and soda-lime silicate glasses.  $\circ$ : silica,  $\bullet$ : soda-lime silicate,  $\square$ :  $45\text{CuO}_x \cdot 55\text{P}_2\text{O}_5$  with  $R(\text{Cu}^+) = 0$ ,  $\blacksquare$ :  $45\text{CuO}_x \cdot 55\text{P}_2\text{O}_5$  with  $R(\text{Cu}^+) = 0.57$ ,  $\triangle$ :  $50\text{CuO}_x \cdot 50\text{P}_2\text{O}_5$  with  $R(\text{Cu}^+) = 0$ ,  $\blacktriangle$ :  $50\text{CuO}_x \cdot 50\text{P}_2\text{O}_5$  with  $R(\text{Cu}^+) = 0.43$ .

indentation size effect (ISE).<sup>19–21</sup> The microscopic mechanism for ISE is still open to discussion,<sup>19–21</sup> and in this paper we do not touch deeply the ISE in our samples. It should be, however, pointed out that the ISE in copper phosphate glasses in the load range of 0.1–1 N is weak compared with silica and soda-lime silicate glasses.

Since the load versus displacement curve during loading corresponds to the consumed energy for the total deformation, it seems to be very important to express the curve using a mathematical function. It was found that all load versus displacement curves in the load range of 0.1–1 N for copper phosphate, silica and soda-lime silicate glasses can be well fitted by quadratic equations,  $P = Ah^2 + Bh + C$ , where  $A$ ,  $B$ ,  $C$  are the constant. Since the universal hardness and elastic recovery of these glasses depend on load as shown in Figs. 5 and 6, it is clear that load versus displacement curves are not expressed by simple quadratic equations of  $P = Ah^2$ . Some typical data are shown in Fig. 7, in which the experimental data and the fitting curves are given. The parameters of  $A$ ,  $B$  and  $C$  in the fitting quadratic equations are summarized in Table 2. It is noted that the parameter  $C$  is small compared with the parameters  $A$  and  $B$ , but is not zero. It was confirmed that at least these parameters are constants for the different loading speeds of 19.6, 49, and 98 mN/s. The results shown in Fig. 7 demonstrate again that the copper phosphate glasses can deform with small energies compared with silica and soda-lime silicate glasses.

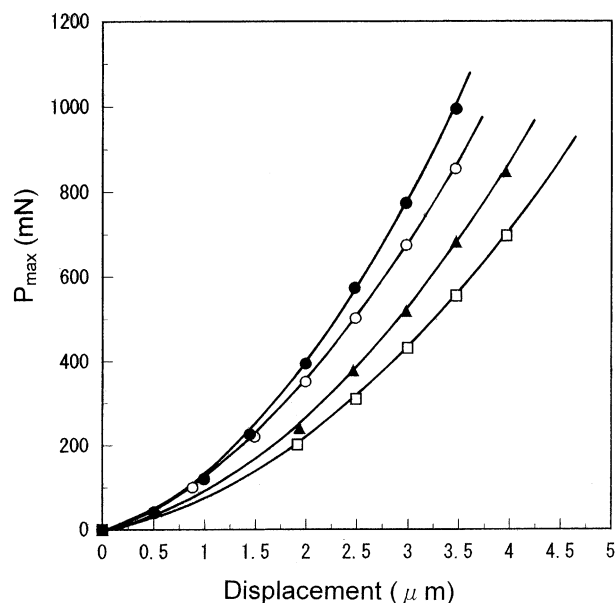


Fig. 7. Correlation between displacement depth  $h_t$  and the maximum load  $P_{\max}$  for copper phosphate, silica and soda-lime silicate glasses.  $\circ$ : silica,  $\bullet$ : soda-lime silicate,  $\square$ :  $45\text{CuO}_x \cdot 55\text{P}_2\text{O}_5$  with  $R(\text{Cu}^+) = 0$ ,  $\blacksquare$ :  $45\text{CuO}_x \cdot 55\text{P}_2\text{O}_5$  with  $R(\text{Cu}^+) = 0.57$ ,  $\triangle$ :  $50\text{CuO}_x \cdot 50\text{P}_2\text{O}_5$  with  $R(\text{Cu}^+) = 0$ ,  $\blacktriangle$ :  $50\text{CuO}_x \cdot 50\text{P}_2\text{O}_5$  with  $R(\text{Cu}^+) = 0.43$ .

Table 2

Values of the parameters in well-fitted quadratic equations,  $P = Ah^2 + Bh + C$ , for load displacement curves obtained by Vickers nanoindentation tests at room temperature in air, where  $P$  is the load and  $h$  is the displacement depth

Glass	$A(\text{mN}/\mu\text{m}^2)$	$B(\text{mN}/\mu\text{m})$	$C(\text{mN})$
$\text{SiO}_2$	48.48	82.31	−5.70
Soda-lime silicate	61.34	78.94	−9.34
$45\text{CuO}_x \cdot 55\text{P}_2\text{O}_5$			
$R(\text{Cu}^+) = 0$	34.18	40.85	−0.45
$R(\text{Cu}^+) = 0.57$	39.71	29.58	−0.28
$50\text{CuO}_x \cdot 50\text{P}_2\text{O}_5$			
$R(\text{Cu}^+) = 0$	29.57	72.69	−1.87
$R(\text{Cu}^+) = 0.43$	42.30	48.45	−1.39

The loading speed was 49 mN/s, and the load range is 0.1–1 N.

### 3.3. Densification in plastic deformation

The plastic deformation at far below glass transition temperature includes densification and plastic flow.<sup>8,9</sup> Densification has been considered to be a more close-packed arrangement of atoms without breaking molecular bonds.<sup>8,9</sup> A portion of the densification is recoverable by annealing at relatively low temperatures below  $T_g$ .<sup>8</sup> On the other hand, plastic flow occurred during loading in indentation tests is an irreversible phenomenon and is caused by shear stress, probably through breaking of chemical bonds.

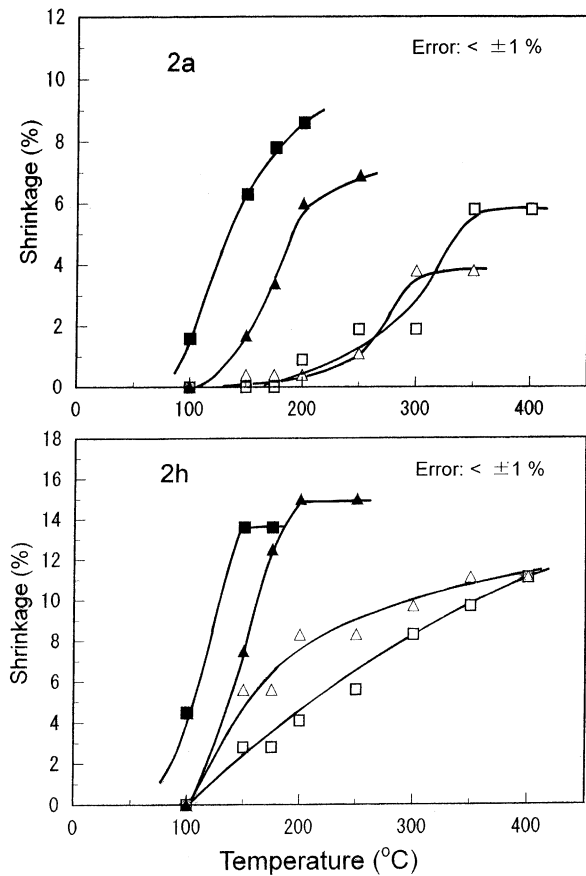


Fig. 8. Fraction of the shrinkages for the diagonal,  $2a$ , and for the distance between counter edges,  $2h$ , in the Vickers impressions as a function of annealing temperature for copper phosphate glasses. The precursor impressions before annealing were obtained by Vickers indentations with a load of 294 mN.  $\square$ :  $45\text{CuO}_x\text{-}55\text{P}_2\text{O}_5$  with  $R(\text{Cu}^+) = 0$ ,  $\blacksquare$ :  $45\text{CuO}_x\text{-}55\text{P}_2\text{O}_5$  with  $R(\text{Cu}^+) = 0.57$ ,  $\triangle$ :  $50\text{CuO}_x\text{-}50\text{P}_2\text{O}_5$  with  $R(\text{Cu}^+) = 0$ ,  $\blacktriangle$ :  $50\text{CuO}_x\text{-}50\text{P}_2\text{O}_5$  with  $R(\text{Cu}^+) = 0.43$ .

Considering the above deformation model in glass, it is very important to clarify the shape change in a residual indentation impression by annealing after unloading. The data in copper phosphate glasses are shown in Fig. 8, in which the fraction of the shrinkages for the diagonal,  $2a$ , and for the distance between counter edges,  $2h$ , in the Vickers impressions are plotted as a function of annealing temperature. The size of the impressions was measured from scanning electron microscope observations. The precursor impressions before annealing were obtained by Vickers indentations with a load of 294 mN. It is seen that the distinct shrinkages in both  $2a$  and  $2h$  are observed in all glasses. It is clear that such shrinkages are observed by annealing at temperatures well below  $T_g$ , demonstrating that densifications which are recovered by annealing occur in copper phosphate glasses as similar to silica and soda-lime silicate glasses.<sup>8,22</sup> Furthermore, it is noted that the fraction of the shrinkage in  $2h$  is much large compared with that in  $2a$ . It should be pointed out that the

shrinkages in the copper phosphate glasses with  $R(\text{Cu}^+) = 0.43$  and  $0.57$  are larger than those in the glasses with  $R(\text{Cu}^+) = 0$ . These results indicate that the copper phosphate glasses with high  $\text{Cu}^+$  contents have a large amount of densification compared with the glasses with low  $\text{Cu}^+$  contents.

## 4. Discussion

### 4.1. Silica and soda-lime silicate glasses

It is well known that the structure of silica glass having no non-bridging oxygens is not compact, but very open, and the strength of Si–O bonds is strong, giving the high glass transition temperature,  $T_g$ , of around  $1200^\circ\text{C}$ . It is, therefore, considered that atoms or structural units ( $\text{SiO}_4$ ) can move without bond breaking even in the condition of relatively large applied loads, but by changing the angle of Si–O–Si bonds during loading. Indeed, a distinct densification (i.e. plastic deformation) has been observed during loading in Vickers indentations of silica glass.<sup>8–10</sup> It is also expected that a structural change during loading recovers largely during unloading due to strong Si–O–Si bonds. This would be the reason for a small universal hardness (in Fig. 5) and a large elastic recovery of around 77% (in Fig. 6) in silica glass. On the other hand, in a soda-lime silicate glass showing around  $T_g = 550^\circ\text{C}$ , a large amount of modifiers ( $\text{Na}_2\text{O}$  and  $\text{CaO}$ ) are included, leading to the formation of non-bridging oxygens and weaker bonds such as  $\text{Na}^+\text{-O}$ . It is, therefore, considered that the structure of soda-lime silicate glass is more compact compared with silica glass. Such structural and bonding features would cause a large permanent deformation, i.e., a small elastic recovery. Indeed, genuine plastic (shear) flow has been observed under indenter loading in soda-lime silicate glasses.<sup>10</sup> As seen in Fig. 5, the universal hardness of silica glass, i.e., the degree of total (elastic + plastic) deformation during loading, is small compared with a soda-lime silicate glass. This demonstrates that silica glass can deform largely during loading. As reported by Kurkjian,<sup>9</sup> however, silica glass has larger Vickers hardness ( $H_v = 7$  GPa at room temperature) compared with a soda-lime silicate glass ( $H_v = 5.5$  GPa). It is obvious that such a difference in the usual Vickers hardness arises from a large difference in the elastic recovery in these glasses.

### 4.2. Copper phosphate glasses

Combined with the results on the elastic recovery (Fig. 6) and the densification (Fig. 7), it is obvious that the plastic deformation is more easily induced during loading in the copper phosphate glasses with high  $\text{Cu}^+$  contents. It is also clear that such a strong tendency to

the plastic deformation due to densification is closely related to the more open glass structure due to the low coordination number of  $\text{Cu}^+$  ions.

The coordination and bonding states of copper ions in copper phosphate glasses are largely different, as demonstrated from XPS measurements in the present study. It is suggested that  $\text{Cu}^{2+}$  ions having an ionic bonding character act as modifier ions, leading to the formation of non-bridging oxygens, but  $\text{Cu}^+$  ions having a covalent bonding character are surrounded by two oxygen atoms and bridge two phosphate chains. The two oxygen coordination state of  $\text{Cu}^+$  has been also proposed in other copper containing glasses such as  $\text{Cu}_2\text{O}\cdot\text{Al}_2\text{O}_3\cdot 4\text{SiO}_2$  and  $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_x$  glasses.<sup>23,24</sup> The structure of  $50\text{CuO}_x\cdot 50\text{P}_2\text{O}_5$  glass with  $R(\text{Cu}^+)=0.43$  is, therefore, considered to be more open compared with the glass with  $R(\text{Cu}^+)=0$ . From these structural features, it is expected that copper phosphate glasses with high  $\text{Cu}^+$  contents show larger elastic recovery than the glasses with low  $\text{Cu}^+$  contents, as similar to silica glass. But, the data in Fig. 5 indicate an opposite trend. As seen in Table 1, the glass transition temperature of  $50\text{CuO}_x\cdot 50\text{P}_2\text{O}_5$  glass with  $R(\text{Cu}^+)=0.43$ ,  $T_g=279^\circ\text{C}$ , is much smaller than that ( $T_g=431^\circ\text{C}$ ) of the glass with  $R(\text{Cu}^+)=0$ . And, it is considered that the introduction of  $\text{Cu}^+$  ions changes the network structure from a three-dimension to a two-dimension. This bonding state in copper phosphate glasses seems to be completely different compared with silica glass, although the copper phosphate glasses with high  $\text{Cu}^+$  contents show large densifications during Vickers indenter loading as similar to silica glass. This would be the reason that the elastic deformation during indenter loading in copper phosphate glasses decreases with increasing  $\text{Cu}^+/\text{Cu}^{2+}$  ratio. It should be also pointed out that the large densification (plastic deformation) in the glasses with high  $\text{Cu}^+$  contents leads to the decrease in the elastic recovery. In the previous paper,<sup>13</sup> it was found that the fracture toughness of the copper phosphate glasses increases with increasing  $\text{Cu}^+/\text{Cu}^{2+}$  ratio. It is concluded from the present study that a strain energy given by a Vickers indenter is consumed through movements of constituent atoms toward open spaces without bond breaking, i.e., through densification. Sato et al.<sup>12</sup> proposed that the single bond strength of  $\text{Cu}^+-\text{O}$  is stronger than that of  $\text{Cu}^{2+}-\text{O}$ , and as shown in Fig. 1, the mean oxygen 1s binding energy increases with increasing  $\text{Cu}^+/\text{Cu}^{2+}$  ratio. This difference might be related to the small difference in the universal hardness shown in Fig. 5.

Phosphate glasses with high transparency for ultraviolet light are becoming important in optical technology, and their structure and physical/chemical properties have been investigated extensively so far.<sup>25</sup> Recently, Kurkjian<sup>26</sup> and Karabulut et al.<sup>27</sup> have studied the mechanical properties of some phosphate glass fibers. To the best of our knowledge, however, there has

been no report on universal hardness and elastic recovery of phosphate glasses except our present study. It is strongly desired to study the correlation between structure and universal hardness/elastic recovery in other phosphate glasses, and such information will lead to designs for glasses with high fracture toughness.

## 5. Conclusion

As described in the introduction, information on universal hardness and elastic recovery of glasses, even for silicate glasses, is lacking compared with the study of other properties such as physical and optical properties. In this study, load/unload displacement curves for  $y\text{CuO}_x\cdot(100-y)\text{P}_2\text{O}_5$  glasses ( $y=45, 50$ ) with different copper valence states, silica and soda-lime silicate glasses at room temperature (humidity  $\sim 64\%$ ) were measured by using a Vickers nanoindentation technique, and universal hardness  $H_u$  and elastic recovery  $E_R$  were estimated in the load range of 0.1–1 N. Copper phosphate glasses have the values of  $H_u=1.7\text{--}2.5$  GPa and  $E_R=0.55\text{--}0.65$ , depending on the  $\text{Cu}^+/\text{Cu}^{2+}$  ratio. The glasses with high  $\text{Cu}^+$  contents show large densification (plastic deformation) during loading and small elastic recovery during unloading compared with the glasses with no  $\text{Cu}^+$  ions. These deformation behaviors are well explained qualitatively by considering lower coordination number and more covalent bonding of  $\text{Cu}^+$  compared with  $\text{Cu}^{2+}$ , which were confirmed from XPS spectra. These results support our previous model<sup>13</sup> on unusual elastic and mechanical behaviors of copper phosphate glasses. The  $E_R$  values of silica glass are around 0.77 and those of soda-lime silicate glass are around 0.63, leading to the smaller  $H_u$  values in silica glass compared with a soda-lime silica glass.

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